# Multiple imputation through machine learning in a survey of sport clubs 

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1. Background [a short description of problem you want to solve with ML and reasons why you want to use ML]

Statistics Poland conducts a census survey of activity of sport clubs which takes place every two years. Survey frame contains 16432 sport clubs of which $1660(10,1 \%)$ requires imputation The data is disseminated on the highest level of spatial disaggregation. Hence the data processing must take that into account.
Methodological Committee (advisory body of president of Statistics Poland) obliged our office to implement multiple imputation in this survey. Thus, we shall test several ML and non-ML methods at multiple imputation task under this project to meet the obligation.
2. Data
2.1 Input data[a short description of input data, an example of how typical data record looks like would be helpful]

Data contains 48 variables of which 44 are count data and 4 are categorical data. The first part of the database pertains to general information about sport club such as members of sport club, persons practising sports, competitors, coaching staff - with respect to age and gender. It can be tackled quite easy with standard methods. The second part of the database covers sport disciplines. Number of them varies among sport clubs and if missing need to be imputed. That part is not covered with this report.
2.2 Data preparation[if there was any data preparation (e.g. data cleaning, text normalisation)]

Not needed. Additional variables e.g. NUTS1-NUTS3 code, locality code and sports association are taken from the survey frame to enhance model results.

### 2.3 Feature selection[if there was any feature selection]

At start, crucial variables were selected:

- Members of sports club
- Persons practising sports
- Competitors

Such a small subset of variables allowed to test the code quickly without hardware burden. Next, other variables from the survey were added to the database. Finally, the database contained 7,000
observations and 13 variables. The table below presents a short description of the variables and their codes in the input file.

Tab. 1. Variables

| CODE | VARIABLE DESCRIPTION | TYPE |
| :--- | :--- | :--- |
| D1W2 | Indicates which sport association does the sport club belong to | categorical |
| D1W3 | Indicates if the sport club participates in the sports competitions | categorical |
| D2W1 | Members of sports club | numeric |
| D2W2 | Persons practising sports | numeric |
| D2W3 | Men practising sports | numeric |
| D2W4 | Men practising sports under 18 years old | numeric |
| D2W5 | Women practising sport | numeric |
| D2W6 | Woman practising sport under 18 years old | numeric |
| D2W7 | Competitors registered in Polish or district sport association | numeric |
| D2W8 | Male competitors | numeric |
| D2W9 | Male competitors under 18 years old | numeric |
| D2W10 | Female competitors | numeric |
| D2W11 | Female competitors under 18 years old | numeric |

2.4 Output data [a short description of how output data looks like]

For each imputation method and set of parameters, we ran 300 simulations and calculated precision measures such as MAE, RMSE, Accuracy and $\mathrm{R}^{2}$. Output data contains precision measures for all simulations.

## 3. Machine learning solution

### 3.1 Models

We tested the following methods:

- MissForest- Nonparametric Missing Value Imputation using Random Forest
- MICE with CART (Classification and Regression Trees)
- MICE with PMM (Predictive Mean Matching)
- MICE with BLR (Bayesian Linear Regression).

MissForest is not a "pure" multiply imputation method as proposed by D. Rubin in 1987. It does not deliver several imputation sets. Nevertheless, it is advocated that it can handle an imputation of mixed data (numeric and factor variables in one data frame). It has an advantage over some other methods that cannot deal both with regression and classification problem. Multivariate Imputation By Chained Equations (MICE) is considered as a principled method of dealing with missing data. The first step of MICE requires a single imputation method to fill in the missing data, the first guess. Since the selection of a single imputation method is arbitrary, we selected three methods: Bayesian Linear Regression (definitely non-ML method), Classification and Regression Trees (definitely ML method) and Predictive Mean Matching (rather non-ML method or hybrid).

### 3.2 Model(s) finally selected and quality criteria used (e.g. accuracy,

time)[which model was selected? What quality measures were used to compare different ML models (e.g. accuracy (e.g. RMSE, MAE, F1, precision), runtime to train the model (e.g. 2 hours for 500,000 training samples and 25 features))]

Let us start with some notation. Assume that $\mathrm{X}=\left(x_{1}, \ldots, x_{n}\right)$ is the vector of true values and let $\mathrm{X}^{*}=$ $\left(x_{1}^{*}, \ldots, x_{n}^{*}\right)$ is the vector of imputed values. For categorical variables (D1W2, D1W3) we calculated accuracy

$$
\operatorname{ACC}(X)=\sum_{I=1}^{n} \operatorname{Ind}(x)
$$

where

$$
\operatorname{Ind}(x)=\left\{\begin{array}{lll}
1 & \text { if } \quad x_{i}=x_{i}^{*} \quad i=1, \ldots, n \\
0 & \text { if } & x_{i} \neq x_{i}^{*} i=1, \ldots, n
\end{array}\right.
$$

For numerical variables D2W1-D1W11 we calculated:

- Mean Absolute Error

$$
M A E=\frac{1}{n} \sum_{i=1}^{n}\left|x_{i}-x_{i}^{*}\right|
$$

- Root of Mean Square Error

$$
R M S E=\sqrt{\sum_{i=1}^{n}\left(x_{i}-x_{i}^{*}\right)^{2}}
$$

- Coefficient of determination (squared Pearson's correlation coefficient).

$$
R^{2}=\frac{\left(\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)\left(x_{i}^{*}-\bar{x}^{*}\right)\right)^{2}}{\sum_{i=1}^{n}\left(x_{i}-\bar{x}\right)^{2} \sum_{i=1}^{n}\left(x_{i}^{*}-\bar{x}_{i}^{*}\right)^{2}}
$$

It should be noticed this definition works well when imputation is unbiased, that is $\bar{x}=\bar{x}^{*}$.
We checked two conditions, that is if D2W2=D2W3+D2W5 and D2W7=D2W8+D2W10. The left-hand side of each equality was treated as true value while the right-hand side of each equality was treated as imputed value. It allowed to calculate aforementioned precision measures.

We also checked if the following inequalities hold:

- men practising sports $\geq$ men practising sports under 18 years old (D2W3 $\geq$ D2W4)
- women practising sports $\geq$ women practising sports under 18 years old (D2W5 $\geq$ D2W6)
- male competitors $\geq$ male competitors under 18 years old (D2W8 $\geq$ D2W9)
- female competitors $\geq$ female competitors under 18 years old (D2W10 $\geq$ D2W11)

For each of them, we calculated the percentage of imputed data such that the given equality holds.

The second criterion of comparison was runtime. The next table shows runtime of simulations for each method. Details of simulation procedure are presented in the next section.

Tab. 2. Runtime of 300 simulations ( 7000 training samples and 13 features) with respect to the share of missing data

| Method | Share of missing data |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $10 \%$ | $20 \%$ | $30 \%$ | $40 \%$ | $50 \%$ |  |
| MissForest | 13 h 28 min | 13 h 29 min | 13 h 30 min | 13 h 30 min | 13 h 31 min |  |
| MICE with PMM | 47 min | 46 min | 39 min | 40 min | 40 min |  |
| MICE with CART | 8 h 12 min | 8 h 15 min | 8 h 20 min | 8 h 17 min | 8 h 8 min |  |


| MICE with Bayesian <br> Linear Regression | 34 min | 35 min | 36 min | 38 min | 42 min |
| :--- | :--- | :--- | :--- | :--- | :--- |

Methods were compared with respect to precision and stability of results, distributional properties and runtime under two different assumption on mechanism of generating missing data. In a case when missing data pattern was Missing Completely at Random (MCAR) all methods achieved quite similar results. However, when missing data pattern was Missing Not at Random (MNAR), precision of the results varied. Moreover, MICE with Bayesian Linear Regression produced unstable and inadmissible results. In terms of precision, MissForest and MICE with CART achieved the best results. Both methods preserved four examined inequalities more often than other two methods. Also, ML methods achieved better distributional properties. The only disadvantage of ML methods is runtime.

Taking into account all arguments, MissForest was chosen for further implementation in our survey.

### 3.3Hardware used[e.g. Intel Core i5-6300u, 2.4GHz]

Intel Core i5-9400 CPU, 2.90GHz
4. Results[result of applying the selected model; if possible, please provide quantitative measures comparing with existing / status-quomethods in terms of accuracy (e.g. manual coding had 0.80 precision), time (e.g. 4,000 hours for manual coding), cost, etc.] Independent of size of imputed data.

In this study we examined two assumptions on mechanism of generating missing data. Under Missing Completely at Random (MCAR) assumption, the probability of being missing is the same only within groups defined by the observed data. Missing Not at Random (MNAR) means that the probability of being missing varies for reasons that are unknown to us and may depend on unobservable data. In a case of MCAR, a given percentage of data was removed at random. In the latter case, all variables were removed except totals, that is, block of variables were removed while crucial variables were left. It is the most common case, when interviewee provides total value without breakdown. We tested a share of $10,20,30,40$ and $50 \%$ of missing data to follow how precision measures changed with decreasing training set. For each mechanism of generating missing data and each share of missing data, 300 simulations were carried out. Some variables from statistical frame were always available.

The following tables show the mean results of MAE and $R^{2}$ for each method. Accuracy was calculated for the variables of the factor type.

Tables 3-6 show the results under MCAR assumption.

Tab. 3. MISSFOREST - MCAR

|  | MAE |  |  |  |  | R ${ }^{\text {/ ACC* }}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 10\% | 20\% | 30\% | 40\% | 50\% | 10\% | 20\% | 30\% | 40\% | 50\% |
| D1W2* | - | - | - | - | - | 0,5971 | 0,5918 | 0,5850 | 0,5750 | 0,5597 |
| D1W3* | - | - | - | - | - | 0,7160 | 0,7117 | 0,7059 | 0,6983 | 0,6878 |
| D2W1 | 21,045 | 20,884 | 21,143 | 21,945 | 23,484 | 0,6465 | 0,6376 | 0,6230 | 0,6087 | 0,5766 |
| D2W2 | 4,858 | 5,943 | 7,392 | 9,317 | 11,965 | 0,9450 | 0,9198 | 0,8910 | 0,8562 | 0,8144 |
| D2W3 | 4,663 | 5,702 | 6,945 | 8,601 | 10,780 | 0,9368 | 0,9033 | 0,8623 | 0,8212 | 0,7791 |
| D2W4 | 7,635 | 8,596 | 9,657 | 10,965 | 12,642 | 0,8891 | 0,8606 | 0,8308 | 0,7911 | 0,7434 |
| D2W5 | 3,325 | 3,954 | 4,721 | 5,762 | 7,097 | 0,8960 | 0,8469 | 0,8031 | 0,7457 | 0,6769 |


| D2W6 | 3,422 | 3,955 | 4,585 | 5,444 | 6,542 | 0,8652 | 0,8216 | 0,7702 | 0,7086 | 0,6331 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :--- |
| D2W7 | 3,772 | 4,895 | 6,318 | 8,190 | 10,713 | 0,9471 | 0,9046 | 0,8574 | 0,7960 | 0,7452 |
| D2W8 | 3,491 | 4,305 | 5,540 | 7,015 | 9,238 | 0,9323 | 0,8923 | 0,8404 | 0,7847 | 0,7194 |
| D2W9 | 3,936 | 4,747 | 5,618 | 6,759 | 8,322 | 0,9404 | 0,9117 | 0,8837 | 0,8412 | 0,7797 |
| D2W10 | 1,484 | 1,791 | 2,218 | 2,766 | 3,561 | 0,9495 | 0,9237 | 0,8856 | 0,8308 | 0,7515 |
| D2W11 | 1,262 | 1,503 | 1,862 | 2,320 | 2,983 | 0,9287 | 0,9040 | 0,8610 | 0,8021 | 0,7127 |

Tab. 4. MICE with Bayesian Linear Regression - MCAR

|  | MAE |  |  |  |  | R ${ }^{2}$ / ACC* |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 10\% | 20\% | 30\% | 40\% | 50\% | 10\% | 20\% | 30\% | 40\% | 50\% |
| D1W2* | - | - | - | - | - | 0,4107 | 0,4091 | 0,4083 | 0,4059 | 0,4042 |
| D1W3* | - | - | - | - | - | 0,5263 | 0,5251 | 0,5219 | 0,5192 | 0,5157 |
| D2W1 | 36,335 | 36,745 | 37,315 | 36,745 | 36,335 | 0,6350 | 0,6031 | 0,5875 | 0,5604 | 0,5344 |
| D2W2 | 4,153 | 7,225 | 10,811 | 7,225 | 4,153 | 0,9724 | 0,9541 | 0,9241 | 0,8892 | 0,8388 |
| D2W3 | 3,370 | 6,070 | 9,216 | 6,070 | 3,370 | 0,9651 | 0,9430 | 0,9088 | 0,8713 | 0,8195 |
| D2W4 | 11,602 | 13,664 | 15,691 | 13,664 | 11,602 | 0,8754 | 0,8330 | 0,7876 | 0,7186 | 0,6413 |
| D2W5 | 2,523 | 3,931 | 5,770 | 3,931 | 2,523 | 0,9244 | 0,9012 | 0,8612 | 0,8014 | 0,7131 |
| D2W6 | 6,098 | 6,857 | 7,597 | 6,857 | 6,098 | 0,8822 | 0,8428 | 0,7962 | 0,7329 | 0,6550 |
| D2W7 | 3,100 | 5,521 | 8,693 | 5,521 | 3,100 | 0,9708 | 0,9499 | 0,9185 | 0,8703 | 0,8166 |
| D2W8 | 2,711 | 5,062 | 7,967 | 5,062 | 2,711 | 0,9645 | 0,9400 | 0,9081 | 0,8537 | 0,7947 |
| D2W9 | 10,228 | 11,711 | 13,312 | 11,711 | 10,228 | 0,8560 | 0,8142 | 0,7625 | 0,6962 | 0,6211 |
| D2W10 | 1,280 | 1,972 | 3,180 | 1,972 | 1,280 | 0,9455 | 0,9236 | 0,8818 | 0,8054 | 0,6944 |
| D2W11 | 3,043 | 3,438 | 3,943 | 3,438 | 3,043 | 0,9030 | 0,8720 | 0,8328 | 0,7629 | 0,6621 |

Tab. 5. MICE with CART - MCAR

|  | MAE |  |  |  |  | $\mathrm{R}^{2}$ / ACC* |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 10\% | 20\% | 30\% | 40\% | 50\% | 10\% | 20\% | 30\% | 40\% | 50\% |
| D1W2* | - | - | - | - | - | 0,5706 | 0,5625 | 0,5850 | 0,5750 | 0,5597 |
| D1W3* | - | - | - | - | - | 0,6971 | 0,6941 | 0,7059 | 0,6983 | 0,6878 |
| D2W1 | 24,620 | 25,140 | 21,140 | 21,940 | 23,480 | 0,6039 | 0,5608 | 0,6230 | 0,6087 | 0,5766 |
| D2W2 | 8,085 | 9,971 | 7,392 | 9,317 | 11,960 | 0,9151 | 0,8737 | 0,8910 | 0,8562 | 0,8144 |
| D2W3 | 7,941 | 9,268 | 6,945 | 8,601 | 10,780 | 0,9056 | 0,8650 | 0,8623 | 0,8212 | 0,7791 |
| D2W4 | 9,235 | 10,400 | 9,657 | 10,960 | 12,640 | 0,8832 | 0,8443 | 0,8308 | 0,7911 | 0,7434 |
| D2W5 | 5,039 | 5,944 | 4,721 | 5,762 | 7,097 | 0,8265 | 0,7727 | 0,8031 | 0,7457 | 0,6769 |
| D2W6 | 4,290 | 5,149 | 4,585 | 5,444 | 6,542 | 0,8391 | 0,7803 | 0,7702 | 0,7086 | 0,6331 |
| D2W7 | 5,929 | 7,337 | 6,318 | 8,190 | 10,710 | 0,9112 | 0,8590 | 0,8574 | 0,7960 | 0,7452 |
| D2W8 | 5,549 | 6,840 | 5,540 | 7,015 | 9,238 | 0,8988 | 0,8278 | 0,8404 | 0,7847 | 0,7194 |
| D2W9 | 4,601 | 5,572 | 5,618 | 6,759 | 8,322 | 0,9260 | 0,8858 | 0,8837 | 0,8412 | 0,7797 |
| D2W10 | 2,084 | 2,414 | 2,218 | 2,766 | 3,561 | 0,8918 | 0,8709 | 0,8856 | 0,8308 | 0,7515 |
| D2W11 | 1,487 | 1,819 | 1,862 | 2,320 | 2,983 | 0,8885 | 0,8500 | 0,8610 | 0,8021 | 0,7127 |

Tab. 6. MICE with Bayesian Linear Regression - MCAR

|  | MAE |  |  |  |  | $\mathbf{R}^{\mathbf{2}} /$ ACC* $^{c \mid}$ |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1 0 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{5 0 \%}$ | $\mathbf{1 0 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{5 0 \%}$ |
| D1W2* | - | - | - | - | - | 0,4313 | 0,4272 | 0,4236 | 0,4201 | 0,4162 |
| D1W3* | - | - | - | - | - | 0,6261 | 0,6172 | 0,6097 | 0,5988 | 0,5872 |
| D2W1 | 71,823 | 67,857 | 71,095 | 70,763 | 72,718 | 0,4059 | 0,3837 | 0,3681 | 0,3511 | 0,3248 |
| D2W2 | 18,626 | 27,746 | 38,888 | 43,927 | 53,104 | 0,8685 | 0,7921 | 0,7048 | 0,6601 | 0,5715 |


| D2W3 | 18,027 | 25,849 | 31,770 | 34,777 | 41,086 | 0,7946 | 0,7011 | 0,6385 | 0,6070 | 0,5318 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :--- |
| D2W4 | 30,537 | 29,503 | 31,139 | 32,576 | 39,974 | 0,6226 | 0,6232 | 0,5963 | 0,5523 | 0,4680 |
| D2W5 | 12,141 | 14,945 | 18,858 | 21,619 | 24,740 | 0,8138 | 0,7436 | 0,6516 | 0,5730 | 0,4848 |
| D2W6 | 14,495 | 14,718 | 17,259 | 18,898 | 21,378 | 0,7303 | 0,6852 | 0,6240 | 0,5523 | 0,4484 |
| D2W7 | 14,604 | 23,088 | 30,620 | 34,956 | 42,528 | 0,8552 | 0,7599 | 0,6752 | 0,6026 | 0,5261 |
| D2W8 | 14,267 | 21,617 | 25,032 | 32,168 | 34,085 | 0,8074 | 0,7079 | 0,6526 | 0,5548 | 0,5077 |
| D2W9 | 24,107 | 24,480 | 27,556 | 28,153 | 29,177 | 0,6438 | 0,6276 | 0,5707 | 0,5453 | 0,4925 |
| D2W10 | 6,586 | 8,348 | 9,299 | 11,398 | 12,275 | 0,8644 | 0,7838 | 0,7110 | 0,5974 | 0,5044 |
| D2W11 | 7,660 | 8,010 | 9,632 | 9,411 | 11,524 | 0,7799 | 0,7239 | 0,6427 | 0,5581 | 0,4504 |

All methods achieved quite similar results with a little advantage of ML methods.
Tables 7-10 show the results under MNAR assumption.

Tab. 7. MISSFOREST - MNAR

|  | MAE |  |  |  |  | $\mathbf{R}^{\mathbf{2}}$ |  |  |  |  |
| :--- | :---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1 0 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{5 0 \%}$ | $\mathbf{1 0 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{5 0 \%}$ |
| D2W3 | 16,143 | 16,167 | 16,160 | 16,129 | 16,141 | 0,7274 | 0,7252 | 0,7261 | 0,7273 | 0,7252 |
| D2W4 | 17,661 | 17,660 | 17,670 | 17,653 | 17,659 | 0,6577 | 0,6572 | 0,6569 | 0,6576 | 0,6573 |
| D2W5 | 15,371 | 15,368 | 15,356 | 15,343 | 15,351 | 0,4415 | 0,4414 | 0,4420 | 0,4414 | 0,4416 |
| D2W6 | 14,321 | 14,326 | 14,317 | 14,301 | 14,306 | 0,3301 | 0,3293 | 0,3287 | 0,3284 | 0,3288 |
| D2W8 | 11,560 | 11,574 | 11,534 | 11,516 | 11,538 | 0,7267 | 0,7253 | 0,7254 | 0,7271 | 0,7252 |
| D2W9 | 12,394 | 12,402 | 12,417 | 12,404 | 12,405 | 0,7006 | 0,7003 | 0,7007 | 0,7006 | 0,7011 |
| D2W10 | 9,987 | 9,994 | 9,989 | 9,972 | 9,970 | 0,3058 | 0,3042 | 0,3044 | 0,3040 | 0,3032 |
| D2W11 | 8,862 | 8,873 | 8,865 | 8,852 | 8,851 | 0,2182 | 0,2153 | 0,2161 | 0,2157 | 0,2149 |

Tab. 8. MICE with CART - MNAR

|  | MAE |  |  |  |  | $\mathbf{R}^{\mathbf{2}}$ |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1 0 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{5 0 \%}$ | $\mathbf{1 0 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{5 0 \%}$ |
| D2W3 | 21,395 | 21,406 | 21,439 | 21,421 | 21,367 | 0,4918 | 0,4805 | 0,4853 | 0,4815 | 0,4845 |
| D2W4 | 20,815 | 20,678 | 20,753 | 20,670 | 20,668 | 0,4888 | 0,4654 | 0,4748 | 0,4652 | 0,4672 |
| D2W5 | 21,693 | 21,633 | 21,687 | 21,653 | 21,660 | 0,0465 | 0,0428 | 0,0446 | 0,0420 | 0,0423 |
| D2W6 | 18,325 | 18,186 | 18,266 | 18,195 | 18,200 | 0,0361 | 0,0341 | 0,0351 | 0,0336 | 0,0340 |
| D2W8 | 13,158 | 13,263 | 13,299 | 13,321 | 13,228 | 0,5068 | 0,4960 | 0,4982 | 0,4994 | 0,5002 |
| D2W9 | 13,208 | 13,338 | 13,264 | 13,338 | 13,329 | 0,5645 | 0,5457 | 0,5555 | 0,5446 | 0,5475 |
| D2W10 | 10,759 | 10,761 | 10,795 | 10,762 | 10,758 | 0,0533 | 0,0493 | 0,0502 | 0,0487 | 0,0494 |
| D2W11 | 8,615 | 8,582 | 8,628 | 8,582 | 8,579 | 0,0427 | 0,0389 | 0,0392 | 0,0380 | 0,0388 |

Tab. 9. MICE with Bayesian Linear Regression - MNAR

|  | MAE |  |  |  |  |  |  |  |  |  |
| :--- | ---: | ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathbf{1 0 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{5 0 \%}$ | $\mathbf{1 0 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{5 0 \%}$ |
| D2W3 | 21,744 | 22,452 | 21,797 | 21,928 | 22,018 | 0,8355 | 0,8457 | 0,8318 | 0,8168 | 0,8146 |
| D2W4 | $1 E+11$ | $1 E+09$ | 30,232 | 55,017 | 746,202 | 0,0101 | 0,2593 | 0,4058 | 0,1769 | 0,0113 |
| D2W5 | 21,744 | 22,452 | 21,797 | 21,928 | 22,018 | 0,0002 | 0,0007 | 0,0002 | 0,0002 | 0,0003 |
| D2W6 | $2 E+12$ | $2 E+08$ | 20,136 | 23,544 | 35,760 | 0,0076 | 0,0252 | 0,0169 | 0,0967 | 0,0020 |
| D2W8 | 12,069 | 12,384 | 12,114 | 12,200 | 12,334 | 0,9055 | 0,9123 | 0,9097 | 0,8992 | 0,9014 |
| D2W9 | $6 E+12$ | $7 E+08$ | 24,896 | 43,290 | 552,930 | 0,0065 | 0,2790 | 0,4196 | 0,1761 | 0,0139 |
| D2W10 | 12,069 | 12,384 | 12,114 | 12,200 | 12,334 | 0,0002 | 0,0007 | 0,0002 | 0,0002 | 0,0003 |

```
\begin{tabular}{|l|l|l|l|l|l|l|l|l|l|l|} 
D2W11 & \(6 E+13\) & \(1 E+10\) & 11,399 & 13,091 & 30,907 & 0,0039 & 0,0478 & 0,0336 & 0,0951 & 0,0019 \\
\hline
\end{tabular}
```

Tab. 10. MICE with PMM - MNAR

|  | MAE |  |  |  |  |  | $\mathbf{R}^{\mathbf{2}}$ |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
|  | $\mathbf{1 0 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{5 0 \%}$ | $\mathbf{1 0 \%}$ | $\mathbf{2 0 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{5 0 \%}$ |
| D2W3 | 17,780 | 17,931 | 17,782 | 17,781 | 17,786 | 0,7411 | 0,7401 | 0,7417 | 0,7417 | 0,7412 |
| D2W4 | 109,747 | 104,900 | 111,004 | 106,054 | 101,921 | 0,0737 | 0,1144 | 0,0723 | 0,0933 | 0,0908 |
| D2W5 | 17,409 | 17,424 | 17,413 | 17,413 | 17,419 | 0,3424 | 0,3446 | 0,3430 | 0,3418 | 0,3415 |
| D2W6 | 21,950 | 23,390 | 22,013 | 21,859 | 21,869 | 0,1025 | 0,1075 | 0,1027 | 0,1061 | 0,1063 |
| D2W8 | 9,298 | 9,299 | 9,292 | 9,286 | 9,295 | 0,7493 | 0,7497 | 0,7496 | 0,7503 | 0,7497 |
| D2W9 | 98,188 | 91,819 | 101,429 | 93,816 | 94,318 | 0,0573 | 0,1059 | 0,0524 | 0,0785 | 0,0715 |
| D2W10 | 8,791 | 8,788 | 8,784 | 8,781 | 8,787 | 0,1798 | 0,1798 | 0,1800 | 0,1793 | 0,1793 |
| D2W11 | 10,696 | 11,420 | 10,723 | 10,706 | 10,530 | 0,0399 | 0,0469 | 0,0399 | 0,0422 | 0,0421 |

In a case when missing data pattern was Missing Not at Random (MNAR), precision of the results varied. Moreover, MICE with Bayesian Linear Regression produced unstable and inadmissible results. Imputed data often was completely out of range of real data. MICE with PMM also produced high errors in a case of several variables. Such anomalies did not occur in outputs of MissForest and MICE with CART. In terms of precision, in the most of cases, MissForest and MICE with CART achieved the best results with respect to each share of missing data for each variable.

We checked if two equalities: D2W2 = D2W3 + D2W5 (Practitioners) and D2W7 = D2W8 + D2W10 (Competitors), held after imputation. The next table presents the results when $30 \%$ of data is missing.

Tab. 11. Results on preserving equalities.

| MCAR |  | MISSFOREST | MICE PMM | MICE CART | MICE BRL |
| :---: | :---: | :---: | :---: | :---: | :---: |
| MAE | Practitioners | 4,716 | 35,624 | 4,716 | 1,196 |
|  | Competitors | 3,292 | 26,611 | 3,292 | 0,763 |
| RMSE | Practitioners | 28,963 | 80,508 | 28,963 | 1,916 |
|  | Competitors | 24,368 | 62,864 | 24,368 | 1,252 |
| $\mathrm{R}^{2}$ | Practitioners | 0,9199 | 0,6757 | 0,9199 | 0,9996 |
|  | Competitors | 0,9034 | 0,6666 | 0,9034 | 0,9997 |
| MNAR |  | MISSFOREST | MICE PMM | MICE CART | MICE BRL* |
| MAE | Practitioners | 5,709 | 0,782 | 16,586 | 0 |
|  | Competitors | 4,903 | 0,563 | 9,502 | 0 |
| RMSE | Practitioners | 42,274 | 28,404 | 105,600 | 0 |
|  | Competitors | 34,405 | 28,997 | 80,259 | 0 |
| $\mathrm{R}^{2}$ | Practitioners | 0,8664 | 0,9356 | 0,5399 | 1 |
|  | Competitors | 0,8384 | 0,8830 | 0,5745 | 1 |

*MAE and RMSE rounded to three digits, R $^{2}$ rounded to four digits

Non-ML methods obtained better results in a case of MNAR with outstanding performance of MICE with BLR. MICE with PMM achieved poor results under MCAR. Nevertheless, preserving equalities is not a crucial criterion since such equalities can be introduced after the multiply imputation is performed.
The next two tables show the percentage of imputed records such that the following inequalities held

- men practising sports $\geq$ men practising sports under 18 years old (D2W3 $\geq$ D2W4)
- women practising sports $\geq$ women practising sports under 18 years old (D2W5 $\geq$ D2W6)
- male competitors $\geq$ male competitors under 18 years old (D2W8 $\geq$ D2W9)
- female competitors $\geq$ female competitors under 18 years old (D2W10 $\geq$ D2W11)

Tab. 12. Results on preserving inequalities under MCAR.

|  | MISSFOREST | MICE PMM | MICE CART | MICE BRL |
| :--- | :---: | :---: | :---: | :---: |
| men practising sports | 0,9704 | 0,7678 | 0,9704 | 0,8085 |
| women practising sports | 0,9519 | 0,6793 | 0,9519 | 0,6956 |
| male competitors | 0,9648 | 0,7032 | 0,9648 | 0,7398 |
| female competitors | 0,9681 | 0,6922 | 0,9681 | 0,7246 |

Tab. 13. Results on preserving inequalities under MNAR.

|  | MISSFOREST | MICE PMM | MICE CART | MICE BRL |
| :--- | :---: | :---: | :---: | :---: |
| men practising sports | 0,9962 | 0,1846 | 0,9168 | 0,6451 |
| women practising sports | 0,9907 | 0,1899 | 0,9505 | 0,7070 |
| male competitors | 0,9771 | 0,1738 | 0,9628 | 0,6053 |
| female competitors | 0,9875 | 0,1918 | 0,9589 | 0,6725 |

ML methods outperformed non-ML methods in each case.

In the last stage of analysis of the results, some properties of distribution of imputed data were examined. Under MCAR assumption, mean of true values and mean of imputed values coincided in most of cases except MICE with PMM. Relative bias did not exceed 5\%. Under MNAR, relative bias was higher in all cases, but with a little advantage of ML methods. Analysis of standard deviation lead to similar conclusions.

Below there are the density plots for real and imputed data for each method when the percentage of missing data was $30 \%$ (variable D2W3).



In a case when missing data pattern was MCAR, all methods achieved quite similar distribution, except MICE with PMM which produced some outliers. However, when missing data pattern was MNAR, distribution got worse for every method, but ML methods produced distribution more similar to distribution of real data than non-ML methods.
5. Code/programming language [e.g. Python, $R$; you can share your code here as a snippet, as separate file attachment or via Github, google Colab (see examples here)]

R language. Code and input data are stored on local servers.
6. Evolution of this study inside the organisation [e.g. Has this study advanced ML within the organisation?Was there any collaboration within the organisation?]

It is the first time when multiply imputation is tested. Some employees have already took their firststeps in this topic during the training conducted in our office.
7. Is it a proof of concept or is it already used in production?[If it is a proof of concept: Was it successful? How will its results prospectively be used in the future?]

### 7.1 What is now doable which was not doable before?

MissForest method from "missForest" R-package allows to perform multiply imputation with a few lines of code. Definitively, even not-advanced R-users can pick up that imputation method in R. Moreover, the imputation results cover also some precision measures without need of manual calculations.

### 7.2 Is there already a roadmap/service journey available how to implement this?

Not yet.

### 7.3 Who are the stakeholders?

Statistics Poland

### 7.4 Fall Back

Current imputation method was challenged and need to be changed. Thus, there is nothing to go back to.

### 7.5 Robustness

MissForest method did not produce results out of range of true values. Non-ML methods produced outliers under MNAR assumption.
8. Conclusions and lessons learned[e.g. ML can be used for editing but one has to have the following points in mind ...]

Machine Learning methods provided more precise outputs than non- Machine Learning methods. The results of data imputation with MICE strongly depended on underlying single imputation method. If it was CART, the results were better, in general, then for non-ML methods, that is Predictive Mean Matching and Bayesian Linear Regression. ML methods produced admissible results without outliers, what was not a case for not-ML methods. Distributional properties of data imputed with ML-methods were also better. ML preserved inequalities well. The only disadvantage of ML-methods, especially MissForest, is computational complexity.

## 9. Potential organisation risk if ML solution not implemented

10.Has there been collaboration with other statistical organisations, universities, etc?

No.
11. Next steps

In our institution there is a need to develop a relevant knowledge and skills to understand the process of building and testing ML models.
12. References or additional resources

